

# Introduction to Finance

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# Taking Stock

- Capital Budgeting process:

1. Given the capital structure find the appropriate discount rate of the firm using WACC

$$r_{WACC} = \frac{E}{E + D}r_E + \frac{D}{E + D}(1 - T)r_D$$

2. Compute the NPV of the project

$$NPV = \sum_{t=0}^T \frac{CF_t}{(1 + r_{WACC})^t}$$

3. Make investment decision using the appropriate investment decision rule.

# WACC

## Financing Weights

$$r_{WACC} = \frac{E}{E + D}r_E + \frac{D}{E + D}(1 - T)r_D$$

- WACC corresponds to the weighted average of  $r_E$  and  $r_D$ .
- Weights correspond to the share of equity in total assets ( $\frac{E}{E+D}$ ) and the share of debt in total assets ( $\frac{D}{E+D}$ ).
- In some cases the share of common equity vs. preferred equity must be distinguished.
- When possible,  $E$  and  $D$  are computed using their **market value**. This is the value that matters for investors.

# WACC

## Cost of Debt

$$r_{WACC} = \frac{E}{E + D}r_E + \frac{D}{E + D}(1 - T)r_D$$

- $r_D$  is the cost of debt. This is the opportunity cost of holding debt of the company.
- $r_D$  is such that given the price of the debt, investors want to keep holding it:  
 $P_{debt} = NPV_{debt}(r_D)$ .
- This is the **yield-to-maturity**:  $r_D = YTM$ .
  - This is the rate an investor would earn by buying the bond at today's price and holding it to maturity.
- The cost of debt vis-a-vis investors is the YTM but this is not the actual cost of issuing debt. The tax shield of debt reduces the effective cost of debt:  $r_D^* = r_D \times (1 - T)$ .

# WACC

## Cost of Equity

$$r_{WACC} = \frac{E}{E + D}r_E + \frac{D}{E + D}(1 - T)r_D$$

- $r_E$  is the cost of equity. This is the opportunity cost of holding firm's equity or the foregone return for investors of holding other firm's equity with similar risk.
- To evaluate the return, one has to use an asset pricing model.
  - The CAPM is one of the most used asset pricing model.
  - The Constant Growth model is an alternative.

# WACC

## Cost of Equity: the CAPM

$$- \underbrace{r_i}_{\text{Expected return of stock } i} = \underbrace{r_f}_{\text{Return of the risk-free asset}} + \underbrace{\beta_i}_{\text{Beta of stock } i} \times \underbrace{(r_M - r_f)}_{\text{Expected risk premium of the market}}$$

- Expected returns depend only on the asset's non-diversifiable (systematic) risk.
- What differentiates expected returns across assets is  $\beta_i$ , a measure of covariation between  $i$ 's return and the market return. It is a measure of non-diversifiable risk.
- $\beta_i = \frac{\text{cov}(r_i, r_M)}{\text{Var}(r_M)}$ .

# WACC

## Cost of Equity: the CAPM

- To compute  $r_E$  using the CAPM, we need:
  1. Which alternative projects should be used to compare the current firm to.
  2. Forecast the returns from investing in these alternative opportunities.

# WACC

## Cost of Equity: the CGM

- The Constant Growth Model, or Gordon model, is an alternative pricing model.
- Assuming the firm's dividend grow at a constant rate  $g$ , we can use the DCF model to forecast returns.
- $r = \frac{DIV_1}{P_0} + g$



# WACC

## Cost of Equity: CAPM vs. CGM

- Both models should give similar estimates but might also differ.
- Which one to chose?
  - CGM sensitive to analysts forecasts of dividend growth (especially over multiple years).
    - Best fit for large companies with stable dividend streams.
  - CAPM assumes only one factor can predict returns.
    - After 40 years of research, many other factors have been found to predict returns.
    - Best fit for companies paying no dividends, or volatile dividends that are hard to predict.
- In practice, the CAPM is more popular.

# WACC

## Cost of Equity: CAPM vs. CGM

	Capital Asset Pricing Model	Constant Dividend Growth Model
<b>Inputs</b>	Equity beta	Current stock price
	Risk-free rate	Expected dividend next year
	Market risk premium	Future dividend growth rate
<b>Major Assumptions</b>	Estimated beta is correct	Dividend estimate is correct
	Market risk premium is accurate	Growth rate matches market expectations
	CAPM is the correct model	Future dividend growth is constant

# WACC

- $r_E$  and  $r_D$  must always be based on **comparable** projects.
- One has to use historical values of comparable projects to chose them.

# Net Present Value

## General Formula

- Once  $r_{WACC}$  and the CF are known, one can compute the NPV.

$$NPV = C_0 + \frac{C_1}{(1+r)} + \frac{C_2}{(1+r)^2} + \dots + \frac{C_T}{(1+r)^T} = \sum_{t=0}^T \frac{C_t}{(1+r)^t}$$

- This formula is always right. Use it for complex CF structures and when the number of period is not too large.

# Net Present Value

## Specific Securities

- Some securities have specific CF payment that are easy to compute.
- Projects' CF structure generally follows a combination of these specific structures:
  - (Growing) Perpetuity.
  - (Growing) Annuity.

# Net Present Value

## Specific Securities

- Growing Perpetuity: a CF payment with an infinite horizon and a constant growth rate  $g$ :

$$PV = \frac{C}{r - g}$$

- Growing Annuity: a CF payment until (finite) time horizon  $T$  and a constant growth rate  $g$ :

$$PV = \frac{C}{1+r} + \frac{C(1+g)}{(1+r)^2} + \dots + \frac{C(1+g)^{T-1}}{(1+r)^T} = \frac{C}{r-g} \left( 1 - \frac{(1+g)^T}{(1+r)^T} \right)$$

- Take  $g = 0$  if the payment is constant.

# Net Present Value

## Important Rules

- Always bring the CF at different horizons at the same period.
  - CF at different points in time cannot be aggregated.
  - It generally happens when a project has a CF profile that combines different types of formula (e.g. an annuity and a growing perpetuity).
- In the above formulas, the first payment is always in year 1. Add manually the CF (e.g. investment) in year 0 if necessary.

# Decision Rules

## Investment Rules

- How to choose to invest in a project? To invest between different projects?
- Different criteria can be used depending on the constraints and on available information.
  - The Net Present Value.
  - The Internal Rate of Return.
    - It is the unknown in:

$$NPV(IRR) = C_0 + \frac{C_1}{1+r} + \frac{C_2}{(1+r)^2} + \dots + \frac{C_T}{(1+r)^T} = 0$$

- The Payback period
  - The amount of time it takes a project to pay back investment.
- How to choose between these alternatives?



# Decision Rules

## Investment Rules

- How to choose between these alternatives?
  - NPV is the most informative and reliable rule: choose it when possible.
  - Information-intensive but necessitates less information than the IRR.
  - The Payback rule requires less information but is less reliable.
  - Good practice is to use several different rules.

# Decision Rules

## Alternative Projects and Limited Funds

- Mutually exclusive projects:
  - Chose the project with the highest NPV.
- When resources are limited:
  - Compute the profitability index of each project:  $\frac{\text{NPV}}{\text{Investment}}$
  - Rank the projects by profitability.
  - Pick projects until resources are exhausted.
- Always discard projects with negative NPV.

# Market Efficiency

- What we have seen in this course relies on the assumption of market efficiency.
- It ensures that the market price reflects all available information, so we can use it to assess cost of capital, risk, prices, etc.
- Relies on investor being fully rational, e.g. all wanting to hold a portfolio on the SML.

# Market Efficiency

- No free lunch, i.e. no arbitrage.
- Prices reflect all available information.
- Prices follow random walks.
- Trade-off between risk and return.
- Active management does not add value.

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## Paradox

# Market Efficiency

- No free lunch, i.e. no arbitrage.
- Prices reflect all available information.
- Prices follow random walks.
- Trade-off between risk and return.
- Active management does not add value.

**Paradox:** Why would anyone participate in the market? (Grossman and Stiglitz, 1980).

# Market Efficiency

## Random Walk

- Observed since the 19th century (Regnault, Le Bachelier): daily market returns follow a random walk.
- Random successive change in returns  $\longrightarrow$  independence of daily returns.
  - Might include a positive drift.
  - e.g. You bet 100\$ on a game: if tails, you win 3% of your investment, if heads, you lose 2.5%.

# Market Efficiency

## Random Walk

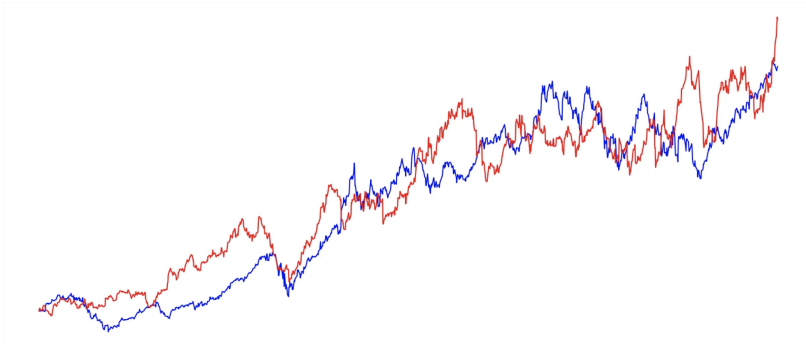
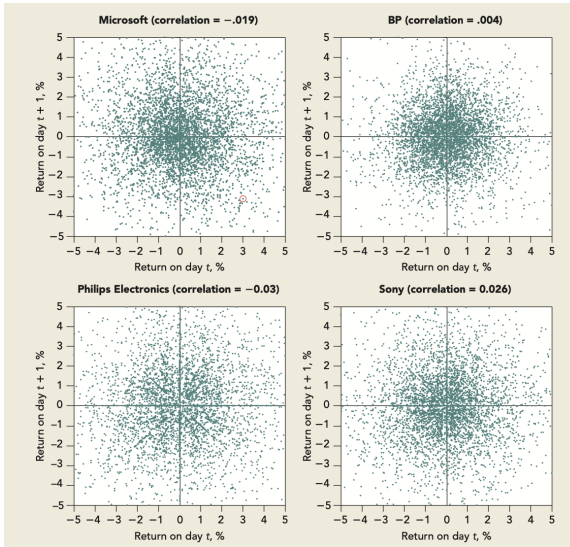


Figure: Stock prices: Apple vs random walk



# Market Efficiency

## Random Walk



# Market Efficiency

## Three forms of efficiency

- **Weak form:** Prices reflect all past trading information.
- **Semi-strong form:** Prices reflect all publicly available information.
- **Strong form:** Prices reflect all public and private information.

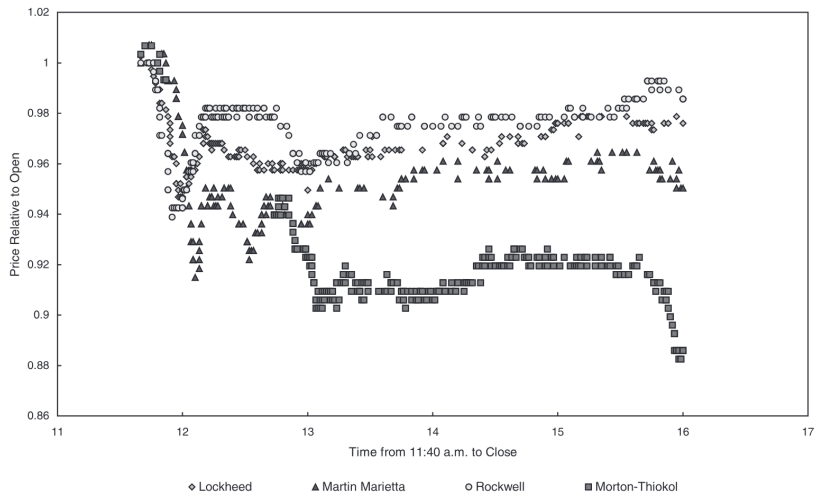
# Market Efficiency

Examples of information incorporated into prices: Challenger

- Challenger exploded at 11:39am on January 28th 1986.
- Big surprise... 6-Months later, the cause of the Crash is made public: one supplier out of four (Morton-Thiokol) was involved (O-rings issue).
- What happened to the price of suppliers in between?

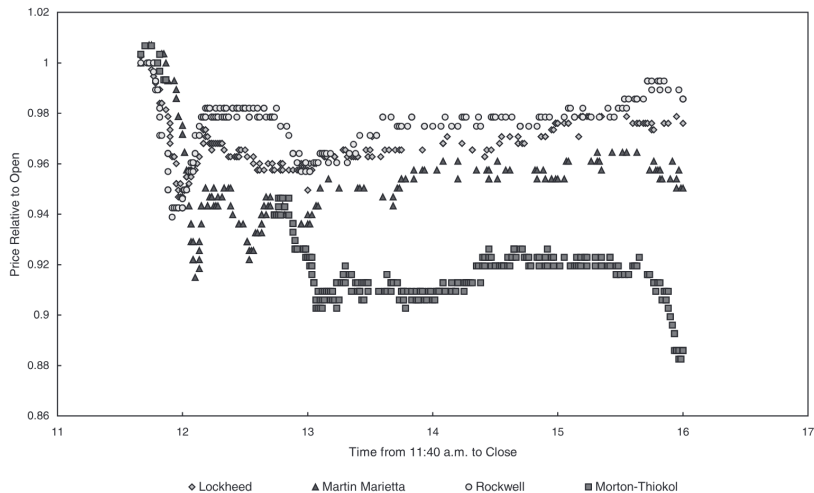
# Market Efficiency

Examples of information incorporated into prices: Challenger



# Market Efficiency

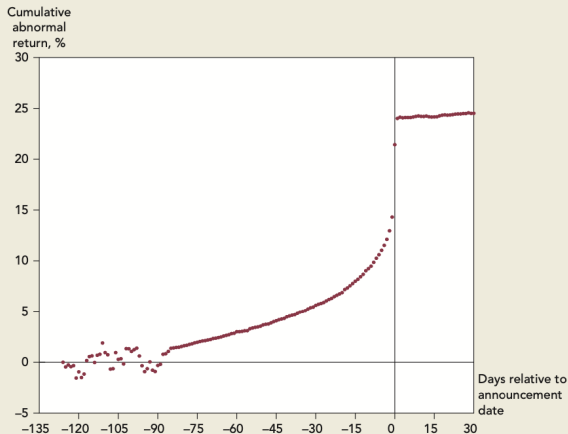
Examples of information incorporated into prices: Challenger



The company lost \$200m  $\approx$  loss is market capitalization.

# Market Efficiency

## Examples of information incorporated into prices: Take-over



**FIGURE 13.4**

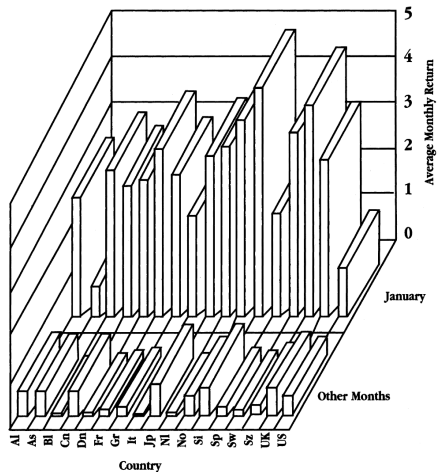
The performance of the stocks of target companies compared with that of the market. The prices of target stocks jump up on the announcement day, but from then on, there are no unusual price movements. The announcement of the takeover attempt seems to be fully reflected in the stock price on the announcement day.

Source: A. Keown and J. Pinkerton, "Merger Announcements and Insider Trading Activity," *Journal of Finance* 36 (September 1981), pp. 855-869. © 1981. Reprinted with permission of Blackwell Publishers Journal Rights. We are grateful to Jinghua Yan for updating the calculations to the period 1979-2004.

# Market Inefficiencies

- Last week: small-firm stocks perform better with respect to risk. Should not be the case if the market were efficient.
- Many other puzzles:
  - Stocks perform better in January.
  - Worse on Mondays.
  - etc.

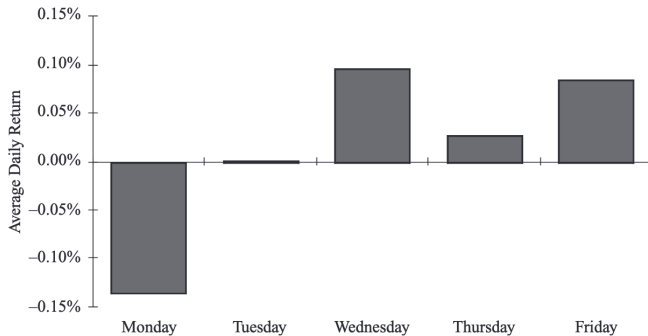
# Market Inefficiencies



**FIGURE 6.15** Returns in January versus Other Months—Major Financial Markets  
*Source:* Gultekin and Gultekin (1983).



# Market Inefficiencies



**FIGURE 6.16** Average Daily Returns by Day of the Week, 1962–1978

Source: Gibbons and Hess (1981).

# Market Inefficiencies

## Bubbles

- Keynes: The stock market is like a casino and agents are guided by “animal spirits”.
- They are not interested in assessing the present value of future dividends and holding an investment for a significant period, but rather in estimating the short-run price movements.
- Not only risk (e.g. quantifiable) but uncertainty. Opinions are based on what other things rather than on actual information → beauty contest. This gives coherence to an irrational behavior.
- Creates speculation and bubbles.

# Market Inefficiencies

## Bubbles

- Speculative frenzy known as bubbles can grow, out of any change in expected profits and dividends.
- Bubbles are self-sustaining: it can be rational to participate. Why?

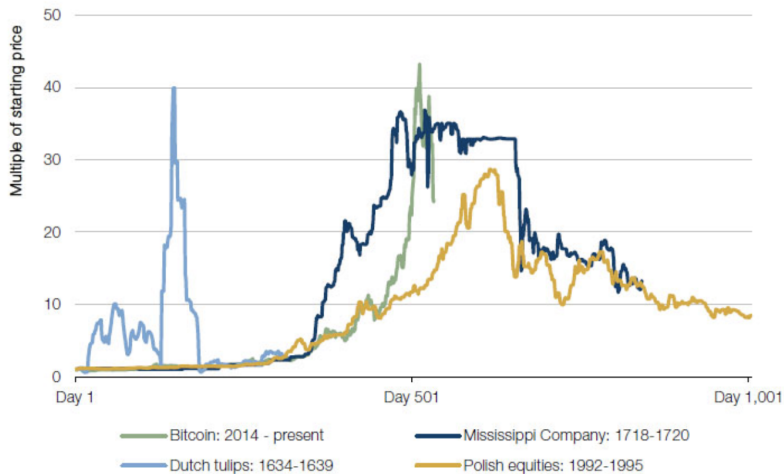
# Market Inefficiencies

## Bubbles

- Speculative frenzy known as bubbles can grow, out of any change in expected profits and dividends.
- Bubbles are self-sustaining: it can be rational to participate. Why?
- If the bubble is expected to continue, investors can make important gains if they are able to cash out for it burst.
- Minsky: Markets are fundamentally unstable because they tend to create bubble when they get optimistic.

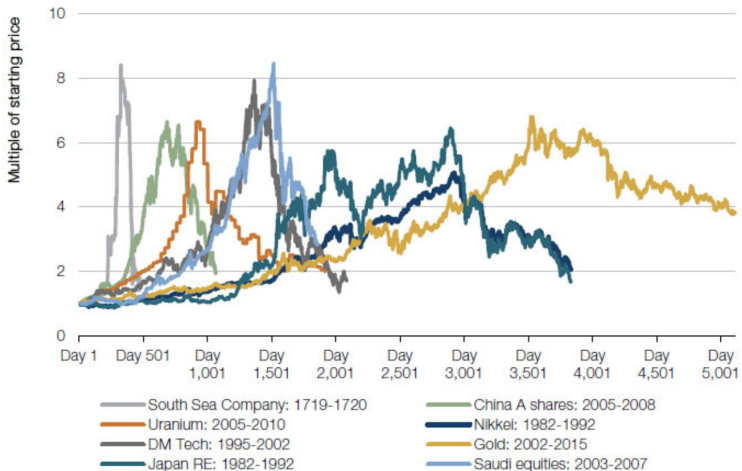
# Market Inefficiencies

## Bubbles



# Market Inefficiencies

## Bubbles



# Market Inefficiencies

## Behavioral Agents

- Do you prefer:
  - A: 240k €
  - B: 1mn € with 25% probability, 0 otherwise

# Market Inefficiencies

## Behavioral Agents

- Do you prefer:
  - C: -750k €
  - D: -1mn € with 75% probability, 0 otherwise



# Market Inefficiencies

## Behavioral Agents

- Do you prefer:
  - A+D: 240k € with 25% probability, -750k € with 75% probability
  - B+C: 250k € with 25% probability, -750k € with 75% probability

# Market Inefficiencies

## Behavioral Agents

- Agents are not (perfectly) rational:
  - Loss aversion → see prospect theory by Kahneman and Tversky.
  - Beliefs about probability.
  - Overconfidence.
  - Framing
  - etc.

# Market Inefficiencies

## Limits to arbitrage

- Experienced investors could take advantages of these biases and then this arbitrage would lead markets to equilibrium.
- But arbitrage is costly: fees, infrastructure, risks, etc.
- Many examples of arbitrage strategies going wrong (eg. VW, LTCM).